

The Identification of Insulin Saturation Effects During the Dynamic Insulin Sensitivity Test

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Abstract: *Background:* Many insulin sensitivity (*SI*) tests identify a sensitivity metric that is proportional to the total available insulin and measured glucose disposal despite general acceptance that insulin action is saturable. Accounting for insulin action saturation may aid inter-participant and/or inter-test comparisons of insulin efficiency, and model-based glycaemic regulation.

Method: Eighteen subjects participated in 46 dynamic insulin sensitivity tests (DIST, low-dose 40-50 minute insulin-modified IVGTT). The data was used to identify and compare *SI* metrics from three models: a proportional model (*SI_L*), a saturable model (*SI_S* and *Q₅₀*) and a model similar to the Minimal Model (*SG* and *SI_G*). The three models are compared using inter-trial parameter repeatability, and fit to data.

Results: The single variable proportional model produced the metric with least intra-subject variation: 13.8% vs 40.1%/55.6%, (*SI_S/I₅₀*) for the saturable model and 15.8%/88.2% (*SI_G/SG*) for the third model. The average plasma insulin concentration at half maximum action (*I₅₀*) was 139.3 mU·L⁻¹, which is comparable to studies which use more robust stepped EIC protocols.

Conclusions: The saturation model and method presented enables a reasonable estimation of an overall patient-specific saturation threshold, which is a unique result for a test of such low dose and duration. The detection of previously published population trends and significant bias above noise suggests that the model and method successfully detects actual saturation signals. Furthermore, the saturation model allowed closer fits to the clinical data than the other models, and the saturation parameter showed a moderate distinction between NGT and IFG-T2DM subgroups. However, the proposed model did not provide metrics of sufficient resolution to enable confidence in the method for either *SI* metric comparisons across dynamic tests or for glycaemic control.

Keywords: Insulin sensitivity, metabolic testing, physiological modelling, parameter identification.

INTRODUCTION

Although it is generally agreed that some saturable insulin action dynamics occur during most insulin sensitivity (*SI*) tests [1-3], the identification of these effects is often crudely handled or ignored [4]. This choice can be attributed to the assumption that saturation effects are not often encountered during the comparatively low insulin concentrations induced during frequently sampled intravenous insulin tolerance tests (FS-IVGTT). Similarly, in hyper-insulinaemic euglycaemic clamps (EIC) the very large insulin doses lead to saturation [2, 3, 5, 6] but saturation effects are still ignored, creating difficulty in comparing results across protocols or EIC insulin doses.

It is important to understand insulin action saturation effects when testing for *SI*, or when adjusting insulin therapy in glycaemic control [7-9]. Commonly used diagnostic tests

that do not use a patient specific dosing protocol, such as the two-hour oral glucose tolerance test or dynamic insulin sensitivity test (DIST) [10-12], may be affected, at least in some cases, by saturation. In particular, differing patient specific volumes of distribution will cause inter-subject variation in concentration for the same dose, and thus, the insulin efficiency may not be measured equally across subjects leading to greater error in these critical values. For example, successive stepped clamp tests with varying glucose or insulin concentrations have yielded significantly different outcome insulin sensitivity metrics for the same individual [5, 6]. Glycaemic regulation may also be improved by understanding insulin saturation, as simple assumptions of unsaturated, proportional action may not be appropriate with very insulin resistant individuals [13, 14].

Fig. (1) shows a typical response curve for the action of drugs or hormones as a function of concentration. The linear response line shows the gradient at the theoretical zero concentration point and measures the infinitesimal increase in action caused by an infinitesimal increase in concentration from zero. The saturation line shows the theoretical

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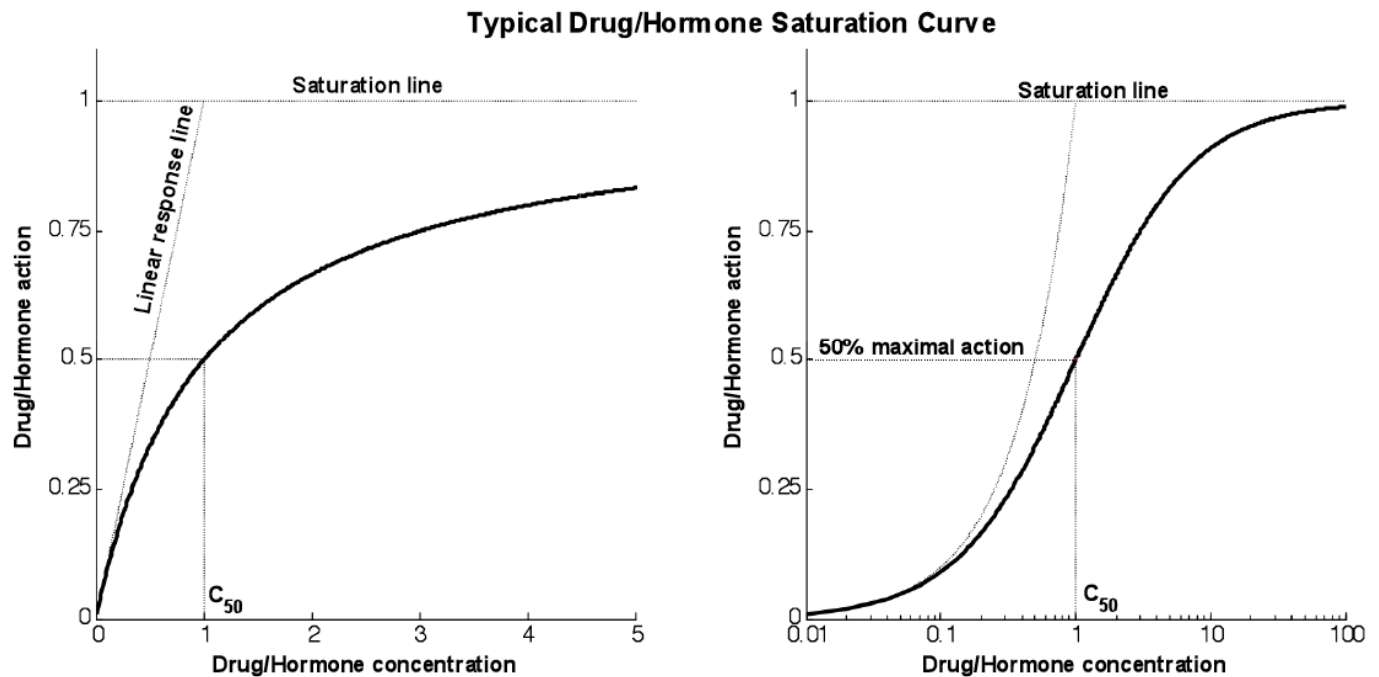


Fig. (1). Typical response curve for any typical saturative drug or hormone. The graphs use proportional and logarithmic x-axis for the same response (linear gradient of 1 and saturation maximum of 1).

maximum action line. The action will asymptotically approach this line as concentration increases and significant saturation effects become apparent.

A typical EIC protocol with a single insulin infusion rate will define a single point on a subject-specific saturation curve. Although equivalence should be given to results along the same saturation curve, it is assumed that equivalence lies on a straight line between this point and the origin. Hence comparing EIC values from differing dosing regimens loses value. Models used during *SI* identification for dynamic tests frequently have linear insulin-dependent terms [11, 15, 16]. Such terms could be represented as linear lines from the origin, with higher sensitivity represented with steeper gradients, and insulin action increasing with concentration with no diminishing returns.

To define saturation effects, the glucose disposal at a series of insulin concentrations must be observed. Previous studies into the saturation of insulin action have used either stepped or multiple EIC tests [2, 6, 17, 18]. The stepped EIC is a long protocol wherein the insulin infusion rate is sequentially changed in a stepwise fashion, usually at 2 hourly intervals for 6-8 hours clamping patients at each steady-state plasma insulin concentration. Studies that used multiple tests have required subjects to have multiple EIC tests on separate days with differing insulin infusion rates. In both cases, increasing insulin doses resulted in decreasing estimates of *SI* for a given subject.

This article presents a method for the identification of a patient-specific insulin concentration at half maximal action (I_{50}) and the theoretical zero insulin gradient (SI_s) of glucose disposal (as a function of glucose availability). Contrary to previously presented studies, the saturation parameters will be identified using a single dynamic test. Hence, the method presented, if successful, offers the advantages of both

reduced testing and reduced (single) test intensity to determine an important patient-specific value.

METHOD

Participants

Participants were recruited under informed consent from the Canterbury and Otago regions of New Zealand to take part in the pilot study of the DIST test [10, 11]. Participant demographics are detailed in Lotz [11]. A total of 18 participants were recruited who represented a range of physiological conditions (age, fitness level and diabetic state) and 46 DIST trials were completed. Study approval was obtained from the Upper South A Regional Ethics Committee for this study.

DIST Test Protocol

Participants reported to the place of testing in the morning after an overnight fast. All participants signed informed consent prior to their first test. A cannula was placed in the ante-cubital fossa from which blood was sampled at $t = 0, 10, 15, 20, 25, 30, 35, 40$ and 50 minutes and boluses of glucose (50% dextrose) and insulin (actrapid) were administered after the $t = 10$ and 20 minute samples respectively. Testing was completed as part of the pilot investigation of the DIST test so the dosing schedule was varied by design. Participants either received a low dose (5g glucose and 0.5U insulin), medium dose (10g -1U), or high dose (20g - 2U) test. Those participants that completed three tests repeated one of the doses. Table 1 summarises the 18 participant's data and defines the NGT (individuals with normal glucose tolerance), and T2DM-IFG (individuals with type 2 diabetes or impaired fasting glucose) subgroups. Impaired glucose tolerance could not be diagnosed with the data available. However, impaired fasting glucose can be identified with the basal sample of the DIST data.

Table 1. Summarised Participant Details, Further Information can be Seen in Lotz *et al.* [10]

	Number (S, m/f)	BMI (kg/m ² , SD)	Test Dose		
			Low	Medium	High
NGT	14 (5/9)	27.0 (6.5)	7	24	5
T2DM-IFG	4 (1/3)	31.2 (4.1)	4	4	2

Physiological Model

A pharmaco-kinetic/pharmaco-dynamic model is used to identify patient-specific parameters from the test data. Equations 1-5 are used to identify a proportional *SI*, as determined by Lotz *et al.* [10, 11].

C-Peptide Pharmaco-kinetics:

$$\frac{dC}{dt} = k_2Y - (k_1 + k_3)C + \xi Uen(t) \quad (1)$$

$$\frac{dY}{dt} = k_1C - k_2Y \quad (2)$$

Insulin Pharmaco-Kinetics

$$\frac{dI}{dt} = -n_K I - \frac{n_L I}{1 + \alpha_I I} - \frac{n_I}{V_p} (I - Q) + (1 - x_L) Uen(t) + \frac{Uex}{V_p} \quad (3)$$

$$\frac{dQ}{dt} = \frac{n_I}{V_q} (I - Q) - n_C Q \quad (4)$$

Glucose-Insulin Pharmaco-Dynamics

$$\frac{dG}{dt} = -p_{gu} (G - G_b) - SI_L (GQ - G_b Q_b) + \frac{P}{V_{g_L}} \quad (5)$$

where: $k_1, k_2, k_3, n_K, n_L, n_I,$ and n_C are rate parameters (min^{-1} or $\text{L}\cdot\text{min}^{-1}$); α_I is the saturation coefficient of liver clearance ($\text{L}\cdot\text{mU}^{-1}$); C and Y are plasma and interstitial compartment C-peptide concentrations ($\text{pmol}\cdot\text{L}^{-1}$); $Uen(t)$ is the rate of endogenous insulin and (equi-molar) C-peptide production ($\text{mU}\cdot\text{min}^{-1}\cdot\text{L}^{-1}$); ξ is a conversion factor ($6.94\text{pmol}/\text{mU}$); I and Q are plasma and interstitial compartment insulin concentrations ($\text{mU}\cdot\text{L}^{-1}$); Uex and P are the insulin and glucose bolus inputs (mU and mmol); V_p and V_q are volumes of distribution (L); x_L is the fractional first pass liver extraction (%); G is the glucose concentration in the plasma ($\text{mmol}\cdot\text{L}^{-1}$); G_b and Q_b are basal levels of the respective species; V_{g_L} is the volume of distribution of glucose (L); p_{gu} is the non-insulin mediated glucose disposal rate (min^{-1}); SI_L is the proportional insulin sensitivity constant ($\text{L}\cdot\text{mU}^{-1}\cdot\text{min}^{-1}$) and the ‘b’ subscript denotes the basal concentration of the respective species.

To generate a saturation model, Equations 4 and 5 must be altered to incorporate appropriate terms. Equations 6 and 7 show how Equations 4 and 5 have been altered to define and include saturation. To enable a consistent treatment of the saturation characteristics of both the insulin absorption to the cell and resultant glucose disposal, the denominators in Equations 6 and 7 must be identical.

$$\frac{dQ}{dt} = \frac{n_I}{V_q} (I - Q) - \frac{n_C Q}{1 + Q / Q_{50}} \quad (6)$$

$$\frac{dG}{dt} = -p_{gu} (G - G_b) - \frac{SI_S GQ}{1 + Q / Q_{50}} + \frac{SI_S G_b Q_b}{1 + Q_b / Q_{50}} + \frac{P}{V_{g_S}} \quad (7)$$

where: Q_{50} is the insulin concentration in the interstitium at half maximal glucose disposal rate ($\text{mU}\cdot\text{L}^{-1}$); V_{g_S} is the volume of distribution of glucose when the saturable parameters are identified and SI_S is the gradient of the saturation curve at the theoretical zero insulin position ($\text{L}\cdot\text{mU}^{-1}\cdot\text{min}^{-1}$).

In addition to these models, the saturable model will be evaluated against a variation of the Minimal Model, which is frequently used for *SI* identification in similar tests [4, 15, 16]. Many model-based methods for determining *SI*, such as the Minimal Model, for dynamic tests utilise a glucose dependant disposal term (*SG*) as a free variable [16]. However, the Minimal Model typically does not model the insulin pharmaco-kinetics in a directly physiological way, particularly in the plasma. Hence, in this study, Equations 1-4 are used to provide the insulin pharmacokinetics for this model. This choice enables a more accurate and fair comparison of *SI* metrics identified from the pharmacodynamics modelled, since the kinetics are equivalent. Equation 8 is used to model the glucose pharmaco-dynamics for this last model, referred to as the *SG* free variable model, as it is not strictly the minimal model.

$$\dot{G} = -SG(G - G_b) - SI_G (GQ - G_b Q_b) + \frac{P}{V_{g_G}} \quad (8)$$

where: *SG* is the identified rate of glucose dependant glucose disposal (min^{-1}); V_{g_G} is the volume of distribution of glucose when the *SG* free variable parameters are identified and SI_G is the proportional *SI* metric derived when *SG* is identified as a variable ($\text{L}\cdot\text{mU}^{-1}\cdot\text{min}^{-1}$)

Identification Process

Insulin sensitivity (*SI*) metrics are identified for each test using the proportional approximation of Equation 5, the saturative expressions of Equations 6-7, and the *SG* free variable model of Equation 8. The first step toward identification of *SI*, is the deconvolution of the C-peptide data using Equations 1 and 2, and the parameters identified using the estimation process outlined in Van Cauter *et al.* [19]. This step produces an endogenous insulin production profile (*Uen*) that is required for all three models presented.

The n_L, x_L, V_{g_L} and SI_L metrics of the proportional model (Equations 3-5) are identified using the iterative integral method [20, 21]. Due to the very high resolution needed to accurately compare the metrics, the number of iterations is increased from 5 to 25. Each iteration of the integral method uses species concentration profiles that have been re-simulated using the parameters identified during the previous iteration. Integrating factors are used for re-simulations when the equations can be linearised (Equations 4, 5, 7 and 8), and quick converging Picard iterations are used other cases (Equations 3, 6) [22, 23]. Thus, highly accurate, patient-specific parameters (n_L, x_L, V_{g_L} and SI_L) and insulin and glucose concentration re-simulations are identified for the proportional model.

The simple iterative integral method is not possible with the saturable variables of Equations 6 and 7 (SI_S , Q_{50} and Vg_S), which are not mathematically separable. Thus, a one dimensional grid search method is used to identify the metrics that minimise the re-simulation 2-norm error to the measured insulin and glucose data. To ensure identification is targeted towards relevant concentrations, the reciprocal of Q_{50} (α_Q , $1/Q_{50}$) is used. Six equally spaced α_Q values are defined on a range between 0 and 0.5 ($L \cdot mU^{-1}$). The range of 0 to 0.5 represents a range of values from the proportional case ($Q_{50}=\infty$) to an unrealistically low saturation threshold ($Q_{50}=2 \text{ mU} \cdot L^{-1}$). Each value is then used in the iterative integral method to identify n_L , x_L , Vg_S and SI_S . The α_Q value that produces the lowest 2-norm error between insulin and glucose simulations and the measured clinical data is used as the centre point of a new search range. The new range is 40% the span of the previous range, but still bounded by 0 and 0.5. Eight such range reductions are iterated and an α_Q value accurate to within 0.1% is identified.

To ensure an equivalent comparison of SI metrics, the SG free variable model uses the same pharmaco-kinetic model for insulin as the proportional model, and so the same n_L and x_L metrics and $I(t)$ and $Q(t)$ simulations are used to identify the sensitivity parameters. Equation 8 is separable in terms of the variables to be identified, and thus, the iterative integral method can be used. However, utilising both SG and SI_G as free variables causes in-stability in identification [24, 25]. Thus, 100 iterations of the iterative integral method are used and the rates of convergence of the SG , SI_S and Vg parameters are slowed and stabilised by averaging the identified value and the values of the previous three iterations, defined:

$$X_{i+1} = (X_{i+1(\text{identified})} + X_i + X_{i-1} + X_{i-2}) / 4 \quad (9)$$

In Silico Verification of Identification Method

To ensure that the method for the identification of saturation parameters is, in fact, identifying meaningful coefficients, and not just fitting to noise, an *in-silico* analysis was completed. Five hundred virtual subjects were simulated with the following evenly distributed ranges: height 1.5-2.3 (m), BMI 18-36 (kg/m^2) and age 18-60 (yrs). A random SI value ($2.5\text{-}30e^{-4} L \cdot mU^{-1} \cdot min^{-1}$) was assigned to each virtual participant and which allowed the a-posteriori parameter estimation defined in [21]. To mimic the in-accuracy of the a-posteriori parameter identification equations, the obtained values were randomised, (normally distributed with a CV of 33% bound between a half and double the original value). The identified a-priori and a-posteriori parameters with Equations 3-5 allow simulation of insulin, and glucose concentration responses to the DIST test stimulus. Virtual samples were taken from the simulated concentration responses at the times defined by the DIST protocol and represented a clean, noise and saturation-free data set.

Normally distributed noise was added to each clean data set in accordance with reported assay errors (glucose CV: intra 2% inter 1%, and insulin CV: intra 3% inter 2%). Each set was used to identify SI using Equations 3-5 and then again using Equations 3, 6 and 7 with Q_{50} fixed at 10000 $mU \cdot L^{-1}$ (using Equations 4-5 assumes no saturation threshold ($Q_{50}=\infty$)). The simulated glucose profiles were then compared to the measured data and the more accurate

Equation set was recorded. The process is repeated 20 times per virtual participant with new noise added to the clean data set at each iteration. Thus 10000 virtual trials are tested.

If the small positive and zero saturation effect terms show equal accuracies across this *in-silico* analysis, but the analysis using the real clinical data shows a significant bias, it could be concluded that the proposed methods are capturing some effect, and not merely noise. Some studies use complex mathematical expressions and methods to define ambiguous or obscure parameters that are often merely functions of noise in the clinical data [26-28]. This analysis could show that the method presented is not doing this. Instead it tests whether, in the presence of noise over synthetic data, no effect (or bias in saturation value) is identified.

Statistical Analysis

An indication of the accurate identification of saturation effects can be found by comparing the bias of the *in-silico* test to the bias found using the clinical data. If the *in-silico* analysis finds a positive saturation in approximately 50% of the cases it will show that the method does not pick up saturation effects when in-fact there is only noise. If the method finds a positive saturation in greater proportions with the real cohort, an observed effect can be confirmed.

The iterative integral method used to identify the variable parameters in each presented model drives the parameter identification by minimising the 2-norm error metric. Thus to best evaluate the applicability of the models, the data-fitting accuracy was identified using the 2-norms of the difference between the measured and simulated insulin and glucose concentrations. For ease of comparison, the mean 2-norm for each species and model is divided by the mean 2-norm for the species from all models. Thus, for each model, a normalised data-fitting error metric is presented for both glucose and insulin simulations enabling a comparison of model performance at a species level.

Furthermore, the inter-test, intra-subject parameter variations are used to show the robustness of metrics of the three models. Equation 10 defines the intra-subject variations.

$$\text{Variability} = \frac{\sum \text{abs}(X_{1..n} - \bar{X})}{n\bar{X}} (\%) \quad (10)$$

The mean inter-subject plasma insulin level at 50% maximal action (I_{50}) is presented to show how the derived metrics compare to the published metrics of stepped, and multiple clamp test investigations [2, 6, 17, 18]. Although glucose disposal is dependent on interstitial insulin, the corresponding plasma level is used to gain equivalence with the findings of previously published stepped clamp investigations. Equation 11 defines the equivalent plasma level at Q_{50} by utilising a steady state ratio of 0.5 between the plasma and interstitium [29-32].

$$I_{50} = 2 \cdot Q_{50} \quad (11)$$

RESULTS

All tests achieved convergence for all identified parameters in all models. No re-simulated profiles were

Table 2. SI Metrics from the Proportional Model, the Proposed Saturative Model and the SG Free Variable Model

Model Parameters		Intra – Subject Variability	Normalised Error I, G	Total Mean (CV)	NGT Mean (CV)	IFG-T2DM Mean (CV)	p-Value
Proportional Model	SI_L^*	13.8%	1.004 1.076	14.38* (61.5%)	16.66* (50.4%)	6.18* (76.2%)	<0.001
Saturation Model	SI_S^*	40.1%	0.991 0.928	36.58* (151.6%)	38.57* (150.9%)	29.42* (157.3%)	0.65
	I_{50}^\dagger	55.6%		139.33† (130.5%)	106.67† (98.9%)	226.4† (131.3%)	0.092
SG free var. Model	SI_G^*	15.8%	1.004 0.996	14.54* (62.1%)	16.91* (50.0%)	5.99* (82.8%)	<0.001
	SG^\ddagger	88.2%		68.10‡ (168.3%)	67.81‡ (184.6%)	69.12‡ (99.3%)	0.97

All metrics are shown as the mean of the full study population metrics and coefficient of variations (CV) of those metrics. Equation 10 defines the intra-subject variation. The mean residual errors produced are derived by finding the mean error between the measured data and the re-simulated profiles for insulin and glucose. The p-values are derived with Student's t-test between the NGT and IFG-T2DM subgroups (* $e^{-4}L \cdot mU^{-1} \cdot min^{-1}$, † $mU \cdot L^{-1}$, ‡ $e^{-4}min^{-1}$).

divergent from the measured data. The 10000 virtual trial *in-silico* analysis showed that the small positive saturation term out performs the linear assumption 49.79% of the time (in terms of fitting accuracy). In comparison, the real clinical data analysis showed that greater accuracy was achieved with a non-zero saturation term 73.9% of the time ($p < 0.002$). Hence, the identification method was robust in the presence of noise and a false effect was not identified.

Table 2 shows the re-simulation accuracy and relative values of the respective terms and models, both as a whole study population and divided into diabetes diagnosis. Fig. (2) shows insulin action profiles from the three models for a typical NGT test participant.

The mean insulin concentration at half maximal action (I_{50}) for the total population was found as $139.3 mU \cdot L^{-1}$ (CV = 130.5%). There were almost significant ($p = 0.092$) differences between the NGT and T2D-IFG subgroups I_{50} values, whereas the SI_S values for these groups were indistinguishable. The SI_L and SI_G parameters showed a difference between these groups whereas the SG term showed no such contrast. Table 3 shows that the I_{50} values found in this analysis were within the wide range of previously published values that were either derived using multiple or stepped EIC protocols [2, 6, 17, 18].

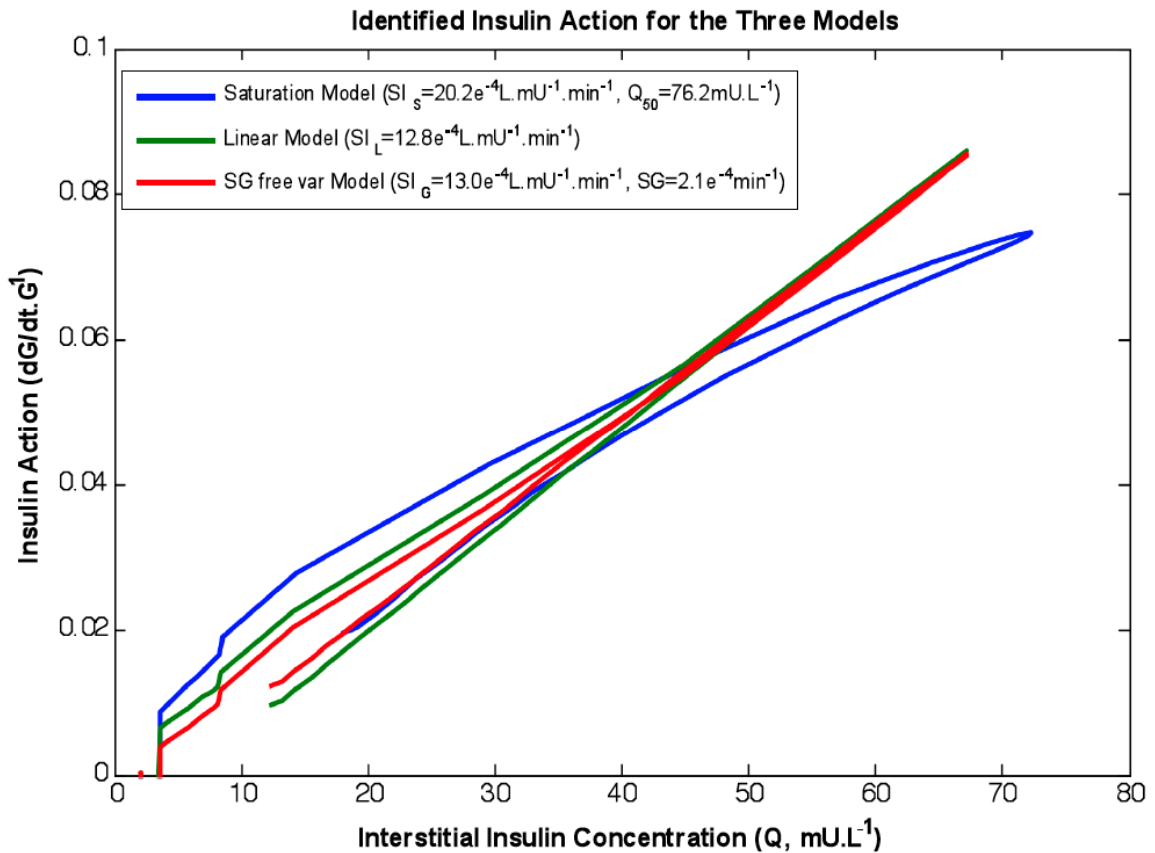


Fig. (2). The rate of change of available glucose as a function of the insulin concentration in the interstitium for the three models identified on the same data set. Note the curved shape of the saturation model captures the behaviour of Fig. (1, left). Furthermore the linear and SG free variable models almost overlay.

Table 3. Mean I_{50} Metrics from a Number of Studies [2, 16-18] Showing the Dependence of Behaviour on Diabetic Progression

Published Findings	Total I_{50} Mean (N)	NGT I_{50} Mean (N)	IFG-T2DM I_{50} Mean (N)	Protocol
Current analysis	139 (33)	107 (23)	226 (10)	Dynamic
Natali <i>et al.</i> [2]	293 (7)	240 (4)	364 (3)	Stepped EIC
Laakso <i>et al.</i> [17]	99 (12)	56 (6)	142 (6)	Stepped EIC
Rizza <i>et al.</i> [18]	-	55 (15)	-	Stepped EIC
Kolterman <i>et al.</i> [6]	221 (20)	130 (7)	270 (13)	Multiple EIC

These values are compared to I_{50} identified with the saturable model.

DISCUSSION

The novel methods presented in this article allow identification of saturation parameters from relatively low-dose, 40-50 minute dynamic tests. However, the intra-subject repeatability of the derived metrics is not of sufficient resolution to promote the use of the method to identify a saturation threshold for an individual. The population trend of higher I_{50} values in the IFG-T2DM subgroup observed in this study has also been reported previously [2, 6, 17].

The saturation model also produced, more accurate numerical data-fitting re-simulations than either the proportional model or the SG free variable model. This result indicates that the method was truly detecting small levels of saturation of insulin action for most participants. This outcome would match expectations given the relatively low dose data available for this study.

The improvement of insulin data fit was slight when considering the additional variable in Equation 6 (Q_{50}). However, there was a significant improvement in the glucose data fit obtained using the saturation model. This would imply that the saturation effect is most evident in the glucose data. Furthermore the glucose model fit error showed the increased fit accuracy possible with the added model variables. However, the saturation variable (Q_{50}) showed a significant further data fit advantage over the added variable of the SG free variable model. Thus implying the presence of saturation effects in the data and the suitability of the saturation model for analysing glucose data.

To date, studies that derive a parameter for saturation have used stepped clamp tests [2], multiple clamp tests [6], or multiple insulin-modified IVGTT tests at various insulin or glycaemic doses [3]. These tests are arduous in terms of clinical intensity and time. A typical three-step clamp protocol will take over six hours of patient and clinician time. Hence, most importantly, this study shows that saturation of insulin sensitivity identification is achievable with a single 40-50 minute test, albeit an identification with a potentially high inter-test variability.

The stepped clamp and multiple clamp studies found physiological I_{50} values for 100% of subjects. However, none of the studies provided an intra-subject repeatability analysis so these results cannot be put further into context. In addition, their much higher insulin doses, well into saturation ranges, provide better resolution to identify this parameter, but also carry increased risk to the participant and thus added clinical burden as well.

The potential reasons behind the poor repeatability of the proposed saturation model are the decreased robustness of the solver in the presence of assay error and physiological and assay noise (such as mixing) [11, 33]. Such noise provokes the interference issues frequently observed when deriving SG and SI with the minimal model [24, 25]. These issues would be exasperated by low insulin doses.

Both the saturation model of Equations 6-7 and the SG free variable model of Equation 8 utilise two free variables to model the glucose decay. Thus, some noise-generated parameter trade-off error is expected. These issues are exacerbated when the free variables in both the saturation and SG free variable models are coupled to the functions of glucose concentration. In simpler terms, while the iterative methods identify the values that minimise the least-square simulation error, the noise in the data causes identifiability issues for multiple free variables, even though the noise-free systems are theoretically identifiable [34].

Table 2 shows that the saturable and SG free variable models produced a higher intra-subject parameter variability than the proportional model. This result is likely to be an artefact of the number of free variables used by the respective models. Indeed, it could be assumed that the saturable model produces results in accordance with what should be expected by models that utilise two free variables to model glucose decay in short duration dynamic tests.

The p-value between the *in-silico* analysis and the real data confirms that the reduction in error is not due entirely to noise fitting. However, the reduction in error could be attributed to the addition of a second free variable. Both the SG free variable and saturation models achieved a lower mean residual error than the proportional model. However, the reduction in error for the SG free variable model was smaller compared to the saturation model. Thus, it could be concluded that if a second variable is to be included and identified, it is more physiologically favourable to identify a saturation variable than the glucose dependant clearance rate (SG).

Improvements in assay techniques may reduce the level of noise in the data. Thus enabling the methods presented to more accurately and repeatably identify these parameters. However, it is likely that the physiological mixing effects that are present during this type of dynamic test will limit any potential improvements obtained by a more accurate assay. This issue would be further compounded by a relatively low sampling rate of 5-10 minutes in the DIST designed to reduce cost and patient/clinical burden [11]. However, it suggests that a modified test protocol with an

increased sampling frequency, larger or repeated boluses may provide better insight or stability in results

Furthermore, the dosing levels of the DIST test were purposefully lower than those used by comparable tests to avoid significant saturation effects, while still allowing detection of a signal and physiological relevance. This low dose, acting as designed, will have partially hidden the saturation effect that this study attempted to measure. The average interstitial insulin concentration reached during the DIST tests ($36.6 \text{ mU}\cdot\text{L}^{-1}$) was significantly below the average identified Q_{50} value. In contrast, most stepped clamp studies achieve plasma insulin concentrations significantly above I_{50} . For example, Natali *et al.* [2] achieved an average plasma insulin concentration of $509 \text{ mU}\cdot\text{L}^{-1}$ with a $200 \text{ mU}\cdot\text{m}^{-2}\cdot\text{min}^{-1}$ infusion and found an average I_{50} of $293 \text{ mU}\cdot\text{L}^{-1}$. This research attempted to identify the saturation effect with data that generally lies toward the linear region of the saturation curve in Fig. (1). Hence a limitation in this study is the lack of higher dose data which was unavailable to better prove the concept. Thus, the proportional model is the most appropriate model to identify metrics from the DIST test.

A significant finding of this study is shown in the p -values for SI_S and α_Q in Table 2. There is virtually no difference between the mean SI_S metrics for the two subgroups ($p=0.65$). However, there is an almost significant difference between the mean I_{50} metrics ($p=0.092$). Physiologically, this result may imply that most people have similar insulin efficiency or sensitivity at the receptor level once insulin has been activated by the cell or at very low concentrations, and observed differences could instead be caused by saturation dynamics. In particular, a lack of receptors may limit sensitivity, and not the binding rate to them. Thus, much of the differences observed in proportional SI metrics from other studies could be affected by these saturation dynamics at cellular and receptor level, particularly if dosing is not patient specific. This hypothesis offers an interesting and physiologically justified insight, but remains to be proven by a purpose driven test.

The mechanisms by which insulin action saturation occurs have not been confirmed. However, most studies which have investigated the matter have promoted either a transportation delay of insulin to the skeletal muscle amongst insulin resistant individuals [3, 32], a lower intensity or availability of insulin receptors at the cell [6], or both [17]. If the former were the case, significant saturation effects would be more prominent in dynamic than steady state tests. The latter would show similar results across protocols. To date no such intra-subject cross-over investigations have been undertaken. However, this study has shown similar findings to the previous clamp investigations, implying that some 'at the cell' effect is likely.

It can be concluded by the reduction in simulation error caused by the incorporation of the saturation parameter that the proportional model (Equations 3-5) does not fully capture some of the subtle variations of the test dynamics. However, it cannot be safely concluded from the analysis presented that it was only saturation effects that caused this error reduction. It is well known that endogenous glucose production (EGP) can become suppressed in the presence of elevated blood glucose and insulin concentrations [35-37].

Although it is assumed that these suppressions have a small effect [38], they may be of similar magnitude to the saturation effects detected in this study. In particular, Equations 5, 7 and 8 assume that basal insulin-dependent and non-insulin-dependent glucose clearance is equal and opposite to EGP (as it is in the basal state) for the duration of the test and is thus cancelled out of the equations. However, the suppression of EGP would result in the opposite effect to saturation; the observed rate of glucose decay would be greater than expected during a period of elevated insulin rather than lesser as occurs with the saturation model. Tracer glucose studies with a purpose-specific test would be required to further delineate this effect, but would also add significant clinical burden and ethical considerations.

CONCLUSION

The novel techniques presented in this article allow a unique identification of a physiologically justifiable, saturation value trend from a single dynamic test at a population level. Despite the robust identification methods, the high intra-patient variability implies that significant development of the protocol is required before high accuracy in saturation parameter identification is possible from single dynamic tests at an individual level. Potential protocol improvements may include larger, and possibly, repeated boluses. The saturation model showed similar accuracy in terms of parameter variation to generally accepted two parameter models, and allowed better fits to the clinical data. However, despite the increased fitting accuracy of the saturation model, the single parameter proportional model is the most stable, and thus it should be used for individual tests.

The comparable sensitivity coefficients between IFG-T2DM and NGT sub-groups with disparate saturation thresholds implies that an 'at-the-cell' effect is the rate limiting factor in glucose disposal. Thus an insulin action saturation threshold may be a significant governing factor of insulin resistance.

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